

Solve for:

$v_i$

$t$ , if  $v_i = 0$

$v_f$

$v$

$L$

$r$

Equation:

$$x_f = x_i + v_i t + \frac{1}{2} a t^2$$

$$x_f = x_i + v_i t + \frac{1}{2} a t^2$$

$$a = \frac{v_f - v_i}{t}$$

$$K = \frac{1}{2} m v^2$$

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$F = \frac{G m_1 m_2}{r^2}$$

$$x_f = x_i + v_i t + \frac{1}{2} a t^2$$

$$v_i t = x_f - x_i - \frac{1}{2} a t^2$$

$$v_i = \frac{1}{t} (x_f - x_i - \frac{1}{2} a t^2)$$

$$x_f = x_i + \cancel{v_i t} + \frac{1}{2} a t^2$$

$$x_f = x_i + \frac{1}{2} a t^2$$

$$\frac{1}{2} a t^2 = x_f - x_i$$

$$t^2 = \frac{2}{a} (x_f - x_i)$$

$$t = \sqrt{\frac{2}{a} (x_f - x_i)}$$

$$a = \frac{v_f - v_i}{t}$$

$$v_f - v_i = a t$$

$$v_f = v_i + a t$$

$$K = \frac{1}{2} m v^2$$

$$v^2 = \frac{2K}{m}$$

$$v = \sqrt{\frac{2K}{m}}$$

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$\left(\sqrt{\frac{L}{g}}\right)^2 = \left(\frac{T}{2\pi}\right)^2$$

$$\frac{L}{g} = \frac{T^2}{4\pi^2}$$

$$L = \frac{T^2 g}{4\pi^2}$$

$$F = \frac{Gm_1 m_2}{r^2}$$

$$\sqrt{r^2} = \sqrt{\frac{Gm_1 m_2}{F}}$$

$$r = \sqrt{\frac{Gm_1 m_2}{F}}$$

# VECTORS

Vectors

- has two parts:

magnitude (number)

direction (H- or compass direction and angle)

Scalars

- has one part  
magnitude

Examples:

acceleration

force

velocity

momentum

displacement

speed

mass

energy

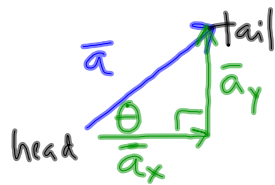
heat

time

pressure

angle

distance

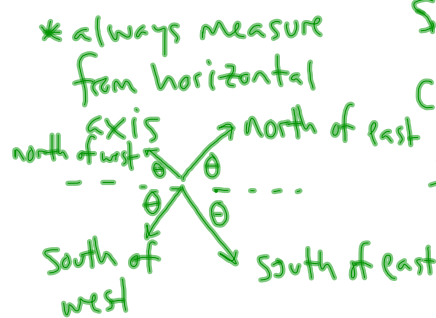


$\langle a_x, a_y \rangle$   
SOH(CAHT)OA

$$\sin \theta = \frac{\text{opp.}}{\text{hyp.}} = \frac{a_y}{a}$$

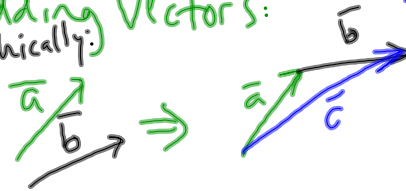
$$\cos \theta = \frac{\text{adj.}}{\text{hyp.}} = \frac{a_x}{a}$$

$$\tan \theta = \frac{\text{opp.}}{\text{adj.}} = \frac{a_y}{a_x}$$



resultant vector:

Adding Vectors:  
Graphically:



goes from head of the first to the tail of the last



Algebraically:  $\uparrow \rightarrow +$

15 m at  $35^\circ$  north of east

20 m at  $30^\circ$  north of east.

$$\vec{a} + \vec{b} = \vec{c}$$

$$x\text{-direction: } \vec{a}_x + \vec{b}_x = \vec{c}_x$$

$$a \cos \theta + b \cos \theta = c_x$$

$$(15 \text{ m}) \cos(35^\circ) + (20 \text{ m}) \cos(30^\circ) = c_x$$

$$c_x = 29.6 \text{ m}$$

$$y\text{-direction: } \vec{a}_y + \vec{b}_y = \vec{c}_y$$

$$a \sin \theta + b \sin \theta = c_y$$

$$(15 \text{ m}) \sin(35^\circ) + (20 \text{ m}) \sin(30^\circ) = c_y$$

$$c_y = 18.6 \text{ m}$$

$$\vec{c} \text{ } 35^\circ \text{ m at } 32^\circ \text{ north of east}$$

$$\hookrightarrow \text{Pythag. thm.} \hookrightarrow \theta = \tan^{-1} \left( \frac{c_y}{c_x} \right)$$